

Planet Mercury: Advance of Perihelion of 43" Seconds of an Arc per Century

By Professor Joe Nahhas
joenahhas1958@yahoo.com

Abstract: Light aberrations equations along the line of sight gives results for the advance of perihelion rates of planets around their mother sun that are better than all published space-time physics and for Planet Mercury, it is equal to 43".0 of an arc per century.

Location \mathbf{r} ----->>Exp ($i \omega t$) ----->> $\mathbf{S} = \mathbf{r} \text{Exp} (i \omega t)$
Orbit \mathbf{r} ----->> light aberrations ----->> Visual Orbit \mathbf{S} ; Exp = Exponential
Where $\omega t = \text{arc tan} (v/c)$
Areal velocity is constant: $r^2 \theta' = h$ Kepler's Law

We have $h = 2\pi a b/T$; $b = a\sqrt{1-\epsilon^2}$; a = mean distance value; ϵ = eccentricity
And $r^2 \theta' = h = S^2 \omega'$

$S = r \text{exp} (i \omega t)$; $h = [r^2 \text{Exp} (2i\omega t)] \omega' = r^2 \theta'$
And $\omega' = (\theta') \text{exp} [-2(i \omega t)]$

Then $\omega' = (h/r^2) [\cosine 2(\omega t) - i \text{sine} 2(\omega t)] = (h/r^2) [1 - 2\text{sine}^2 (\omega t) - i \sin 2(\omega t)]$
And $\omega' = \omega'(x) + i \omega'(y)$; $\omega'(x) = (h/r^2) [1 - 2\text{sine}^2 (\omega t)]$

$\Delta \omega' = \omega'(x) - (h/r^2) = -2(h/r^2) \text{sine}^2 (\omega t) = -2(h/r^2) (v/c)^2$; $\omega T = \text{arc tan} (v/c)$
And (h/r^2) (Perihelion/Periastron) = $[2\pi a \cdot a\sqrt{1-\epsilon^2}]/Ta^2 (1-\epsilon)^2 = [2\pi\sqrt{1-\epsilon^2}]/T (1-\epsilon)^2$
 $\Delta \omega' = [\omega'(x) - h/r^2] = -4\pi \{[\sqrt{1-\epsilon^2}]/T (1-\epsilon)^2\} \text{sine}^2 (v/c)$ radian per second

$\times \{[180/\pi; \text{degrees}] \times [100 \text{years} = 36526 \text{days; century}] \times [3600; \text{seconds in degree}]$

$\Delta \omega'' = (-720 \times 36526 \times 3600/T) \{[\sqrt{1-\epsilon^2}]/(1-\epsilon)^2\} [\text{sine arc tan} (v/c)]^2$
Seconds of arc per century

The circumference of an ellipse: $2\pi a (1 - \epsilon^2/4 + 3/16(\epsilon^2)^2 - \dots) \approx 2\pi a (1 - \epsilon^2/4)$; $R = a (1 - \epsilon^2/4)$
 $v = \sqrt{[G m M / (m + M) a (1 - \epsilon^2/4)]} \approx \sqrt{[GM/a (1 - \epsilon^2/4)]}$; $m \ll M$; Solar system

Advance of Perihelion of mercury.

$G = 6.673 \times 10^{-11}$; $M = 2 \times 10^{30} \text{kg}$; $m = .32 \times 10^{24} \text{kg}$
 $\epsilon = 0.206$; $T = 88 \text{days}$; $c = 299792.458 \text{ km/sec}$; $a = 58.2 \text{ km/sec}$

Calculations yields:
 $v = 48.14 \text{ km/sec}$; $[\sqrt{1-\epsilon^2}] (1-\epsilon)^2 = 1.552$

$$\Delta w'' = (-720 \times 36526 \times 3600 / 88) \times (1.552) [\sin \arctan(48.14 / 299792)]^2 = 43.0'' / \text{century}$$

all right reserved